

Unit 6 | QUANTITATIVE GENETICS

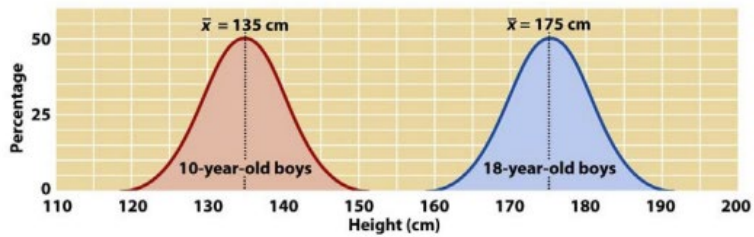


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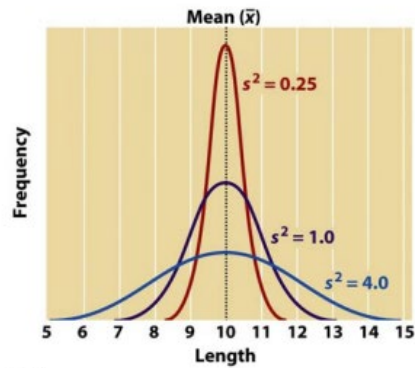
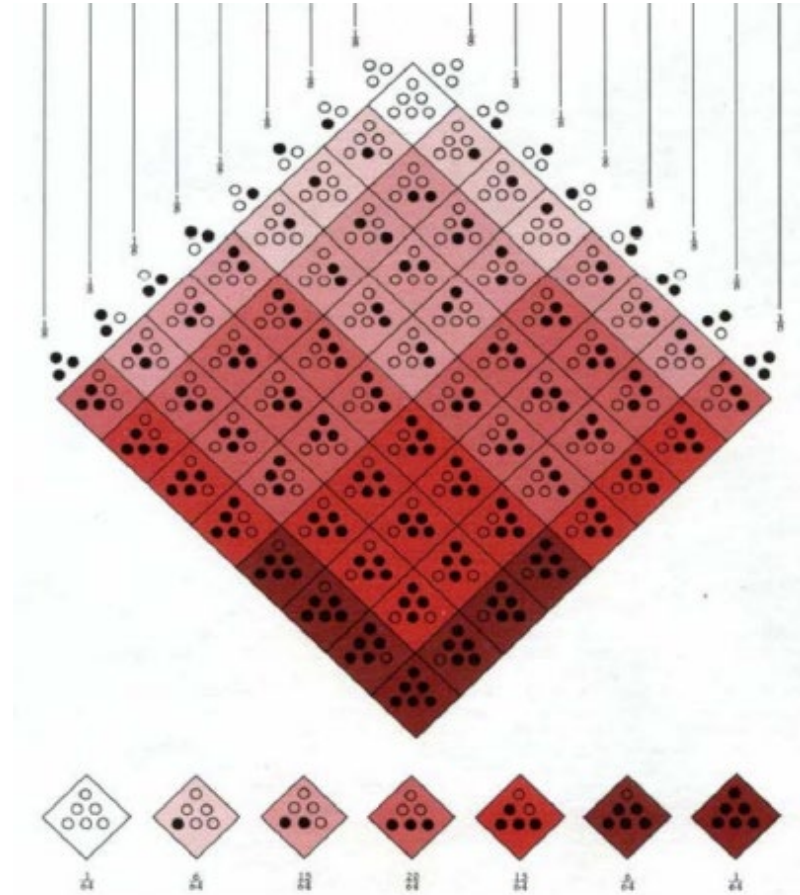


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Biometry vs Mendelian Genetics

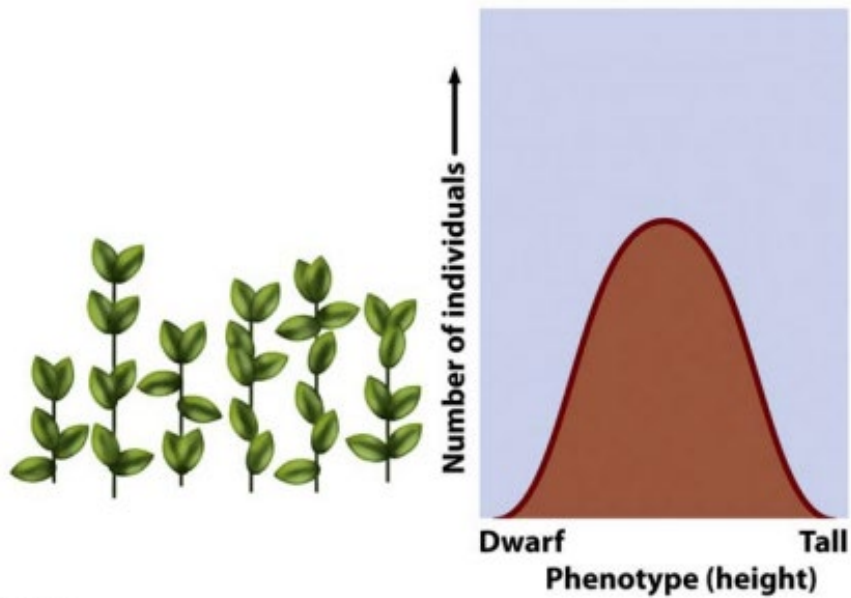
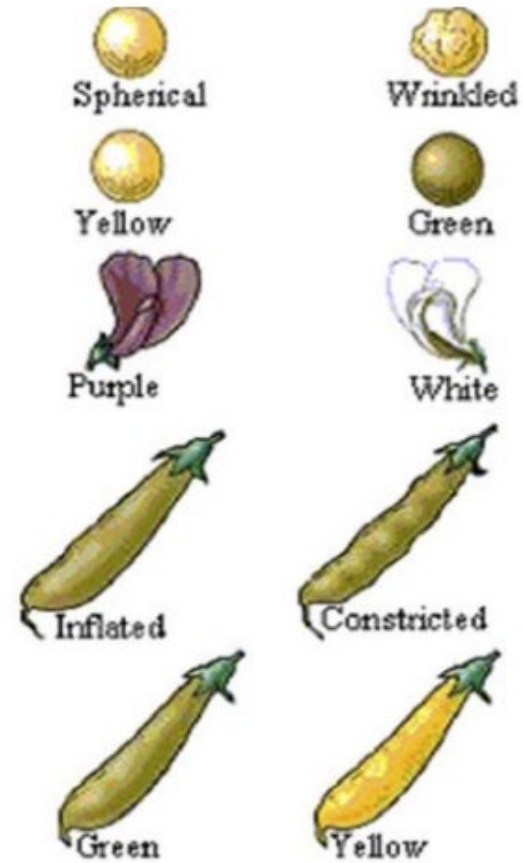


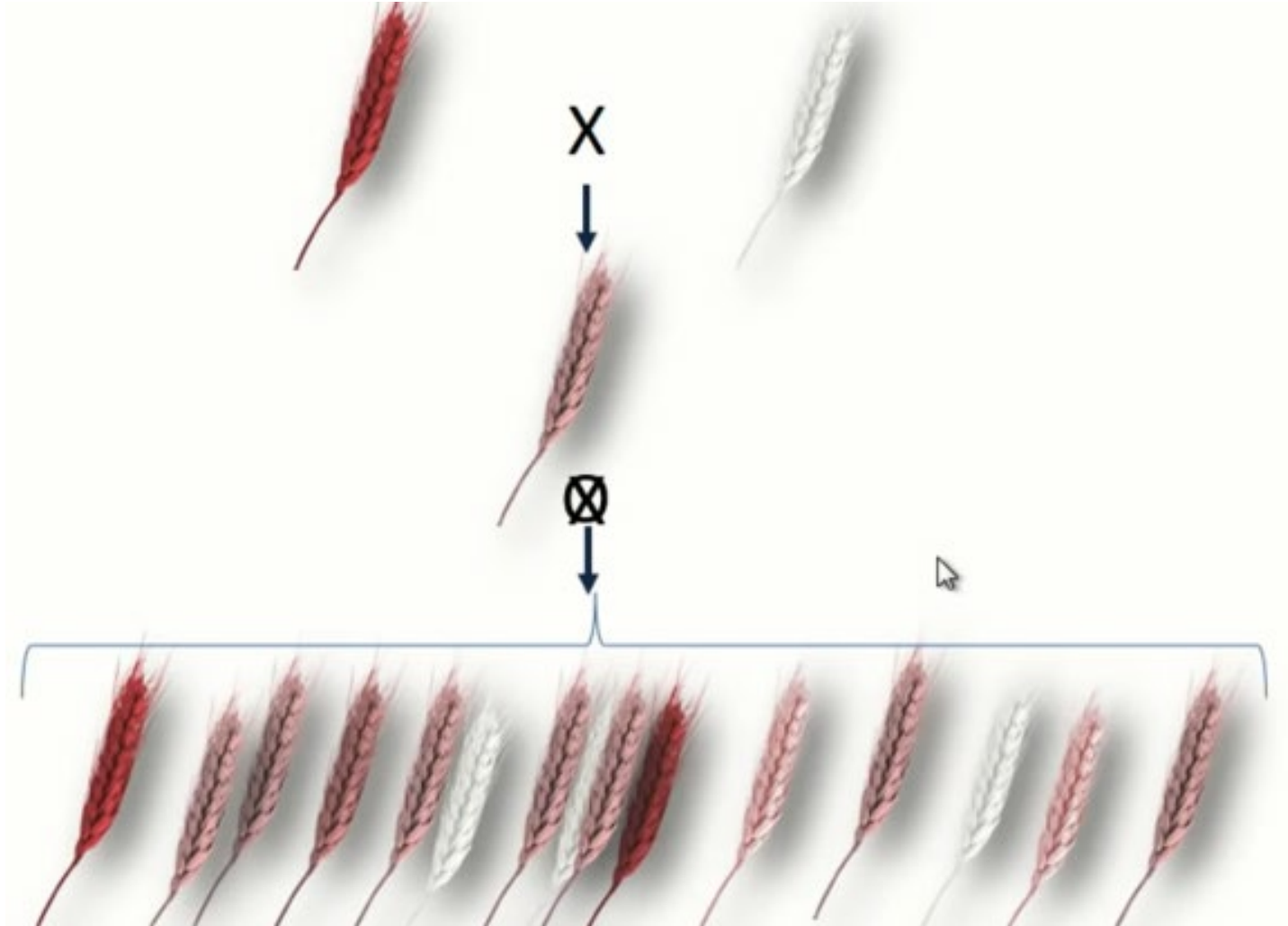
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Continuous variation

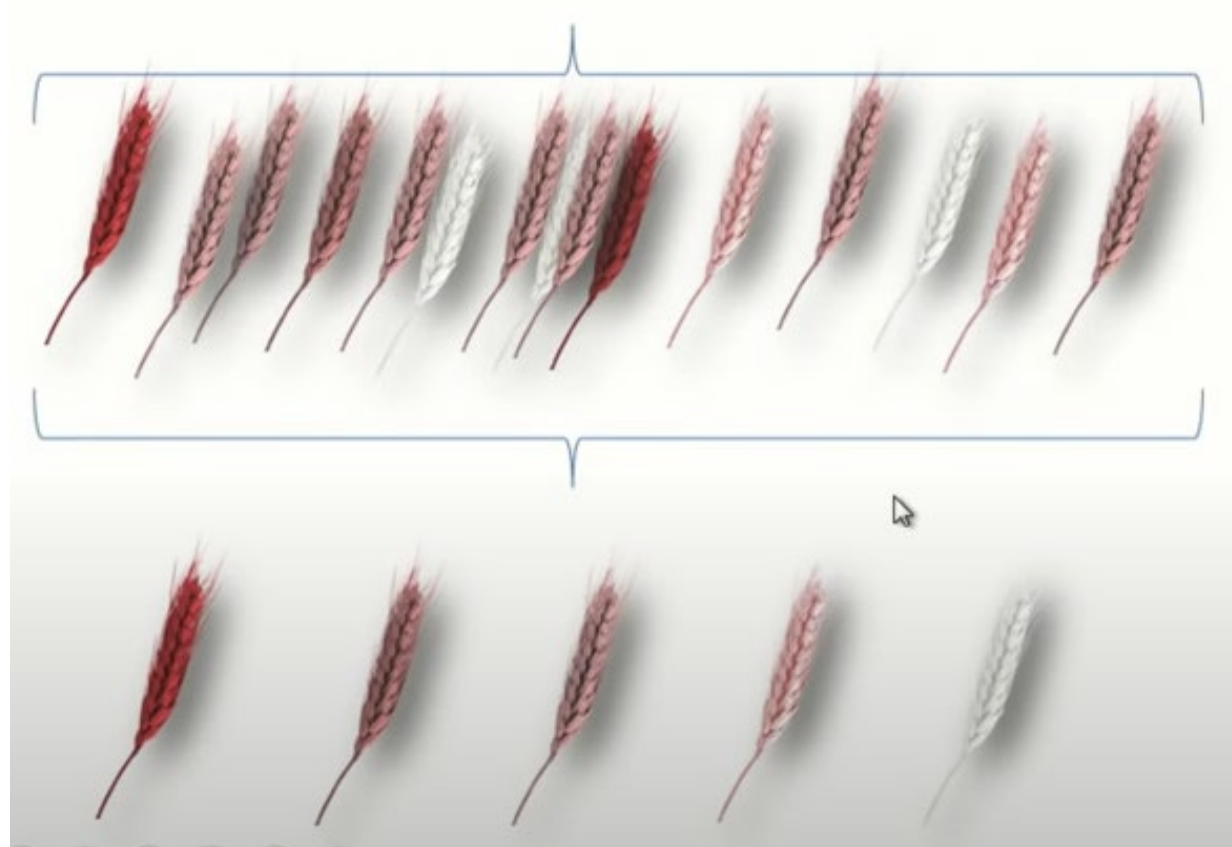


Discontinuous variation

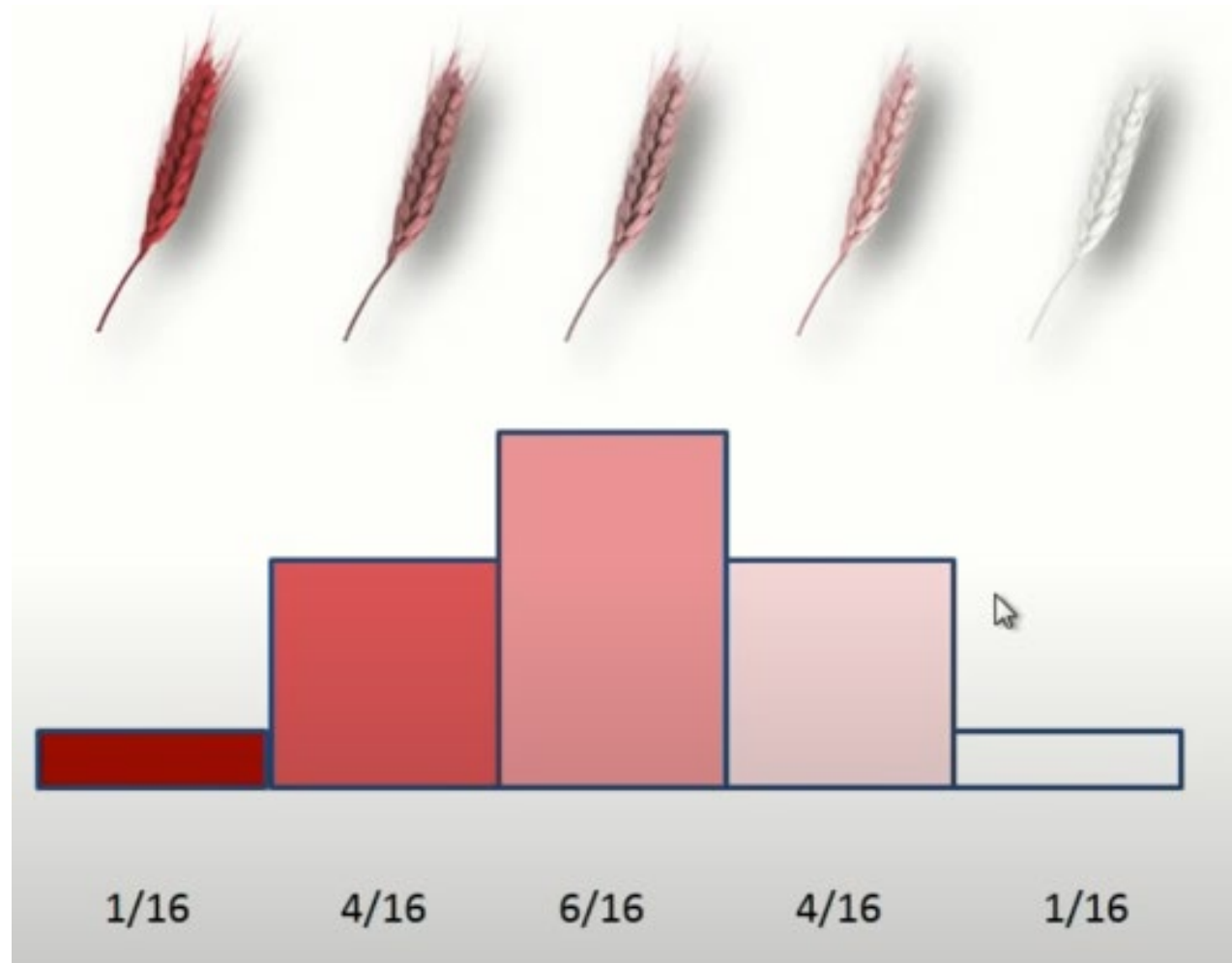
Nilsson-Ehle Experiment (1909)



Nilsson-Ehle Experiment (1909)

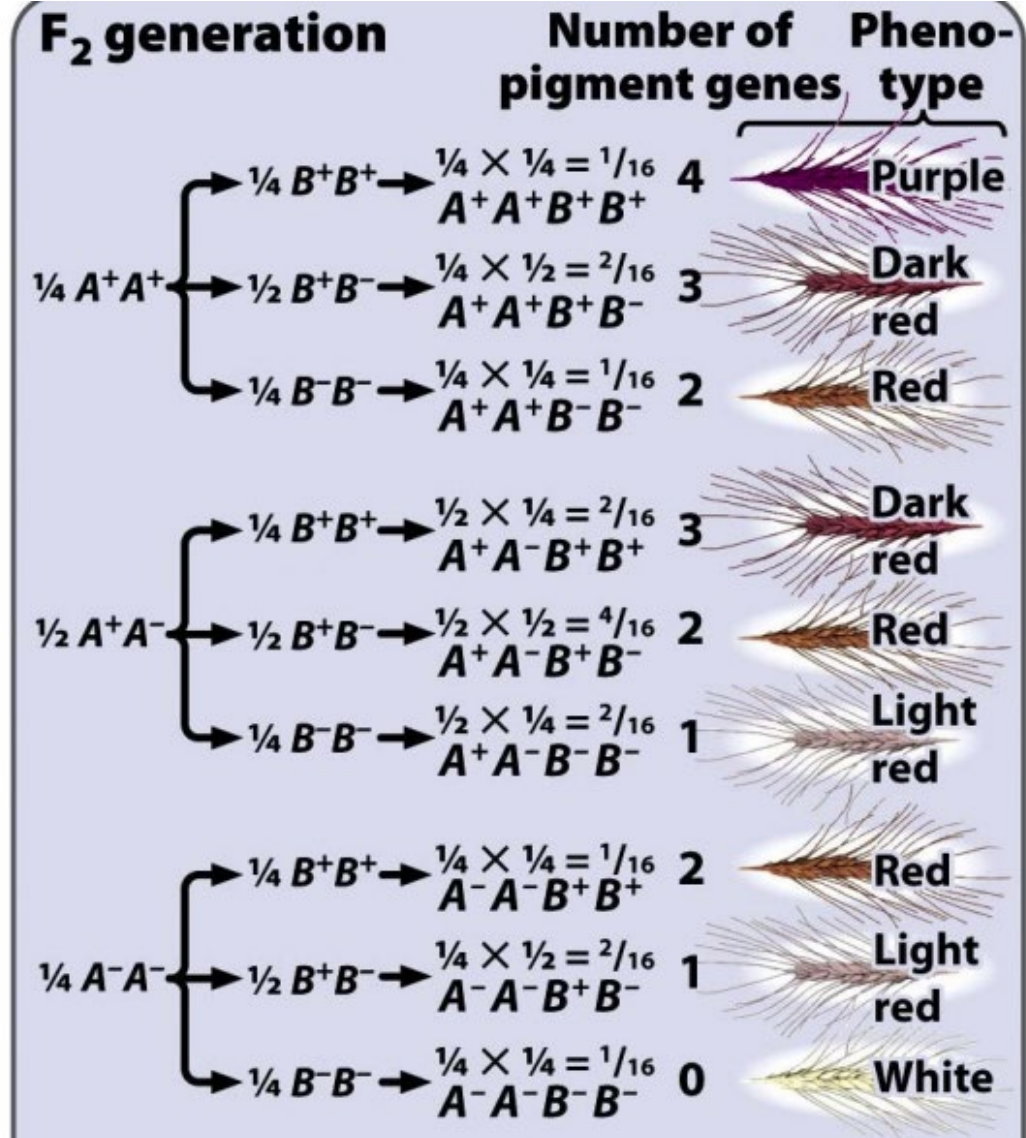
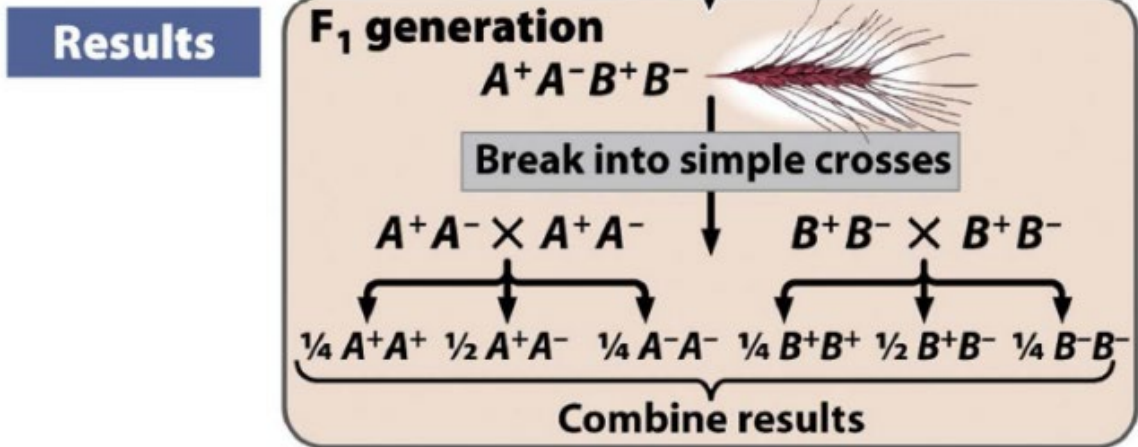
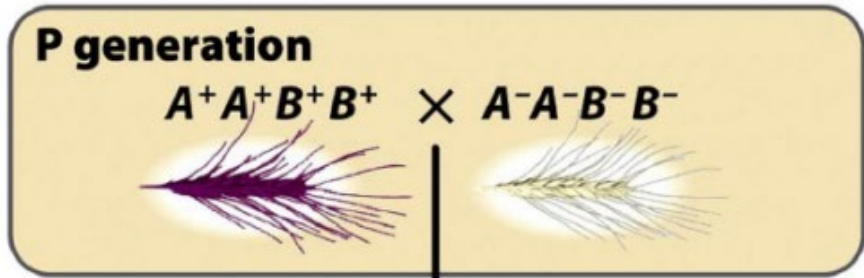


Nilsson-Ehle Experiment (1909)








Nilsson-Ehle Experiment (1909)

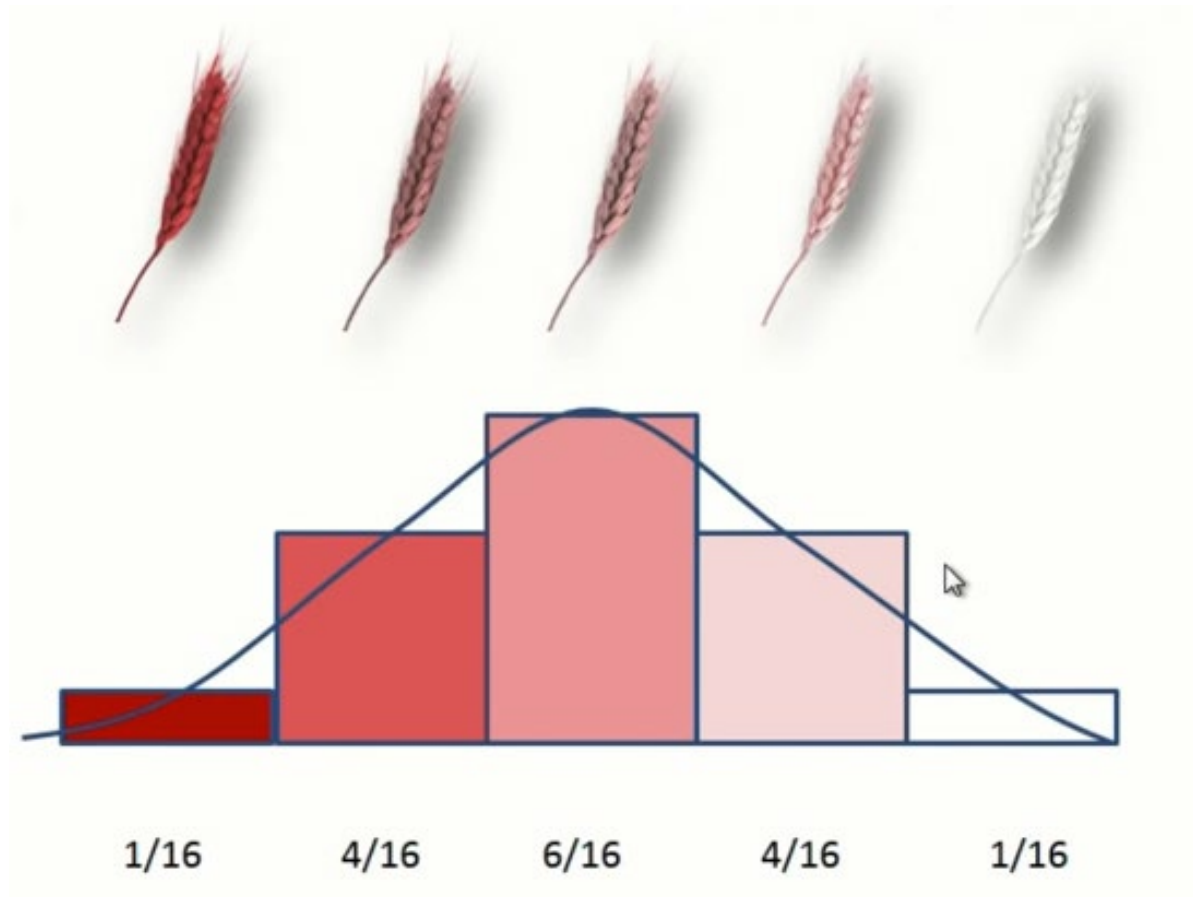
Methods Cross wheat having white kernels and wheat having purple kernels. Intercross the F₁ to produce F₂.



Nilsson-Ehle Experiment (1909)

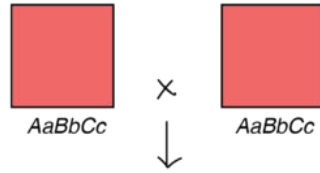
F₂ ratio	Number of	Phenotype
Frequency	pigment genes	
1/16	4	 Purple
4/16	3	 Dark red
6/16	2	 Red
4/16	1	 Light red
1/16	0	 White

Nilsson-Ehle Experiment (1909)



Additive Model:

- Trait due to several genes: polygenic.
- There are additive and non-additive alleles (**additive alleles** contribute to the expression of the trait; **non-additive alleles** don't).
- The contribution of additive alleles is similar and small.



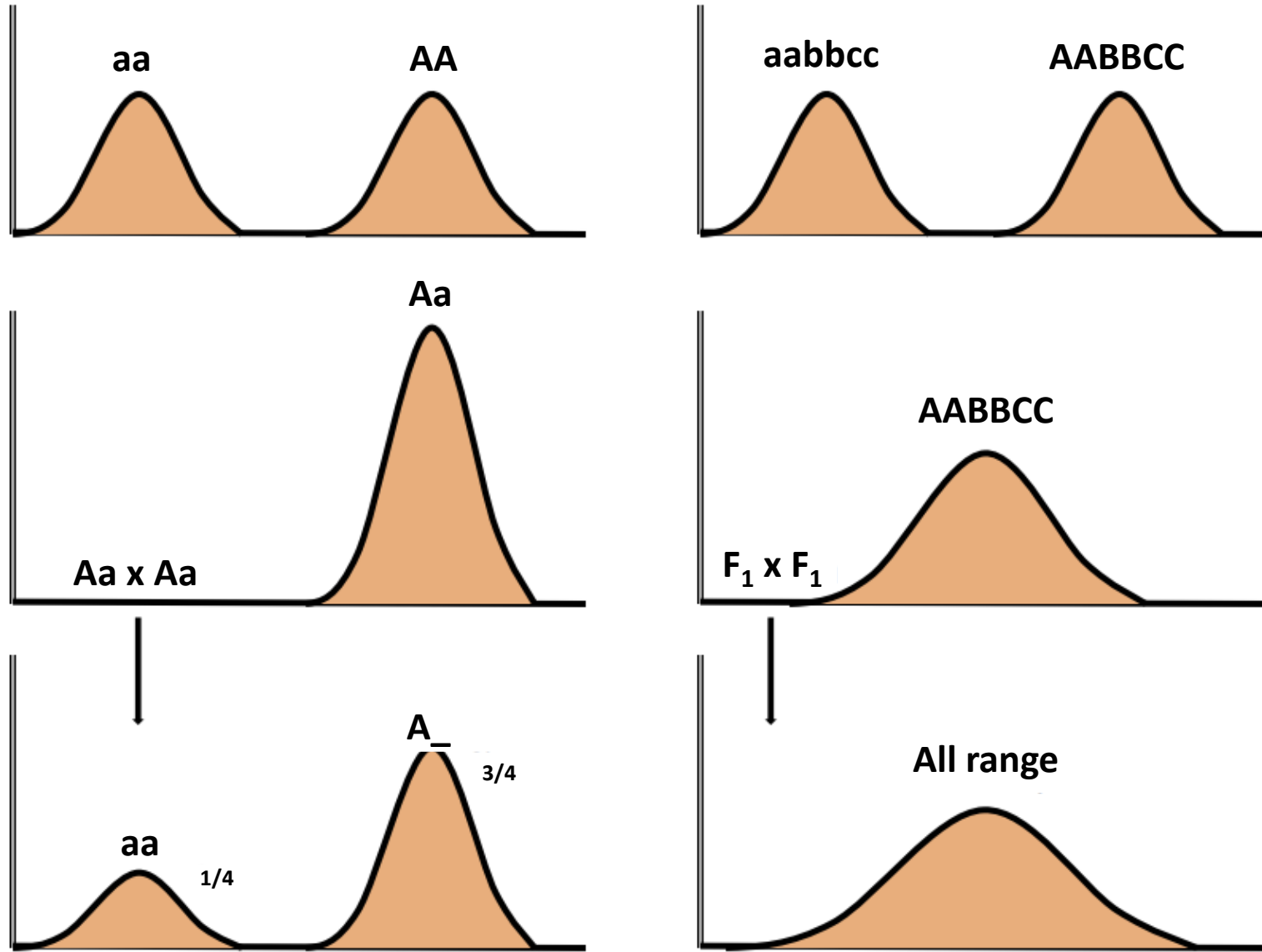
Each uppercase allele (A, B, C) contributes 1 unit of pigment

	ABC	AbC	aBC	ABc	Abc	abC	aBc	abc
ABC	AABBCC	AABbCC	AaBBCC	AABbCc	AAbbCc	AaBbCC	AaBBcC	AaBbCc
AbC	AABbCC	AAbbCC	AaBbCC	AABbCc	AAbbCc	AabbCC	AaBbCc	AabbCc
aBC	AaBBCC	AaBbCC	aaBBCC	AaBBcC	AaBbCc	aaBbCC	aaBBcC	aaBbCc
ABc	AABbCc	AABbCc	AaBBcC	AABBcc	AABbcc	AaBbCc	AaBBcc	AaBbcc
Abc	AABbCc	AAbbCc	AaBbCc	AABbcc	AAbbcc	AabbCc	AaBbcc	Aabbcc
abC	AaBbCC	AabbCC	aaBbCC	AaBbCc	AabbCc	aabbCC	aaBbCc	aabbCc
aBc	AaBBcC	AaBbCc	aaBBcC	AaBBcc	AaBbcc	aaBbCc	aaBBcc	aaBbcc
abc	AaBbCc	AabbCc	aaBbCc	AaBbcc	Aabbcc	aabbCc	aaBbcc	aabbcc



1 : 6 : 15 : 20 : 15 : 6 : 1

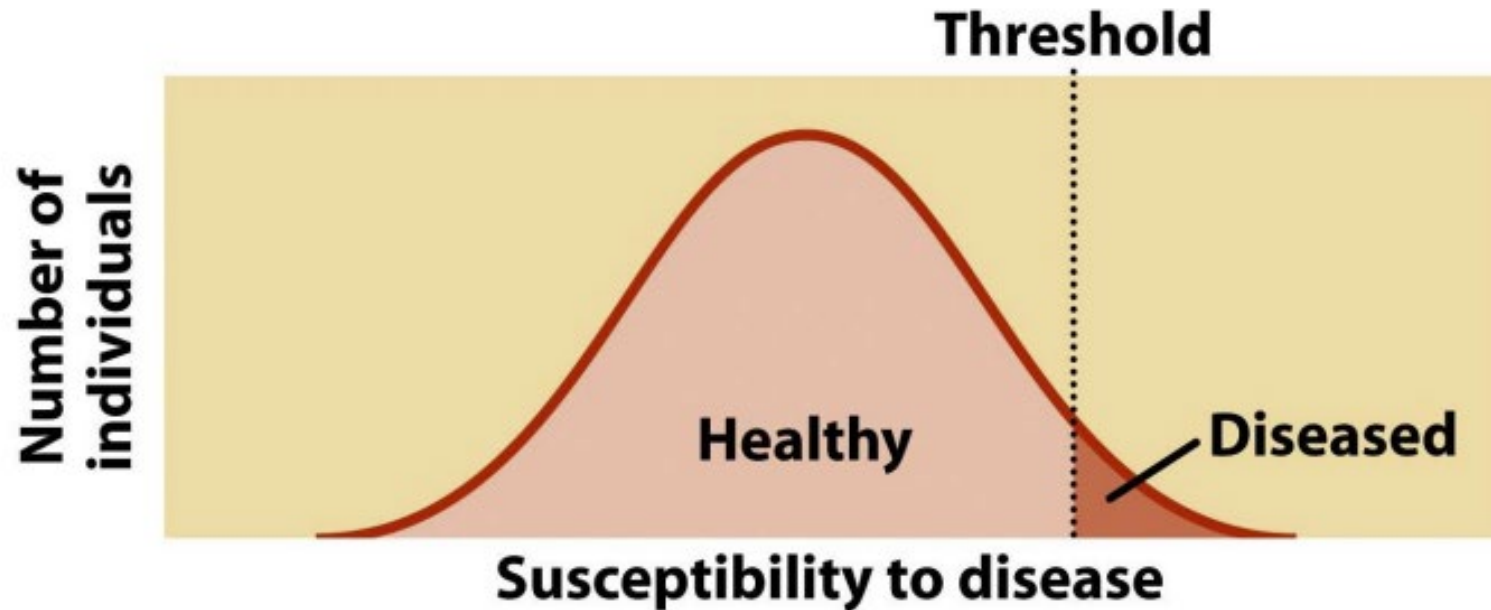
Qualitative vs Quantitative



Meristic Traits: quantitative traits depending on polygenes but organised in closed categories.



Threshold Traits: quantitative traits that are discretely expressed in a limited number of phenotypes (usually two).

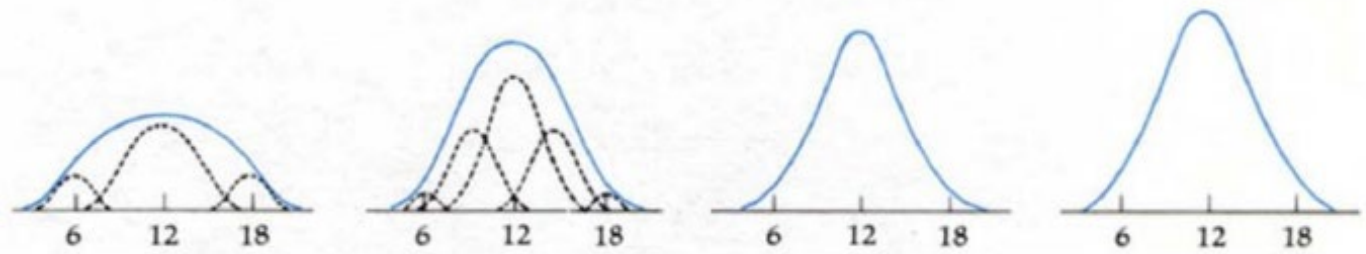
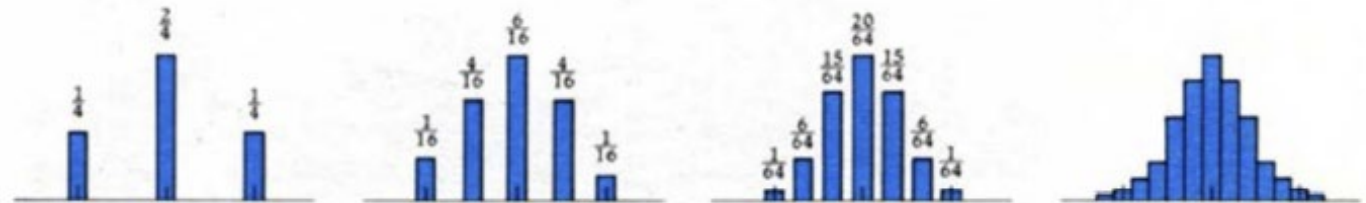
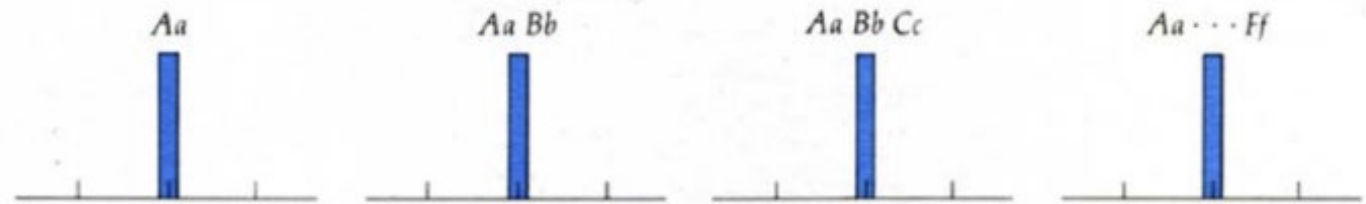
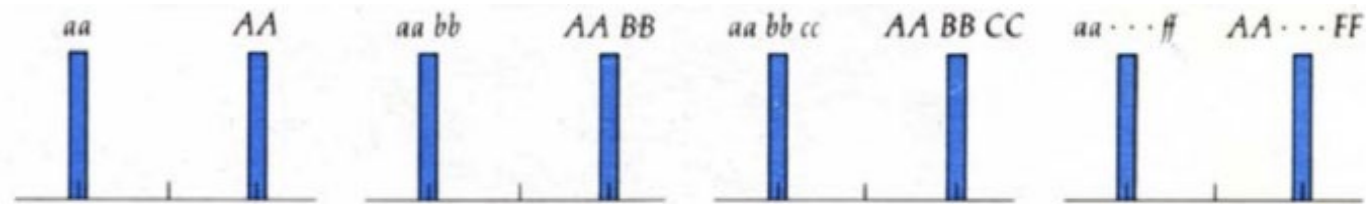


Questions of Quantitative Genetics

- **Can we make predictions** on how many individuals with a particular phenotype we might expect?
- **How many genes** are involved in a particular trait?
- What portion of observed variability is due to a **genetic differences** between individuals? What portion is due to **environmental factors**?
- Where are these genes **located in the genome**?

Questions of Quantitative Genetics

- **Can we make predictions** on how many individuals with a particular phenotype we might expect?



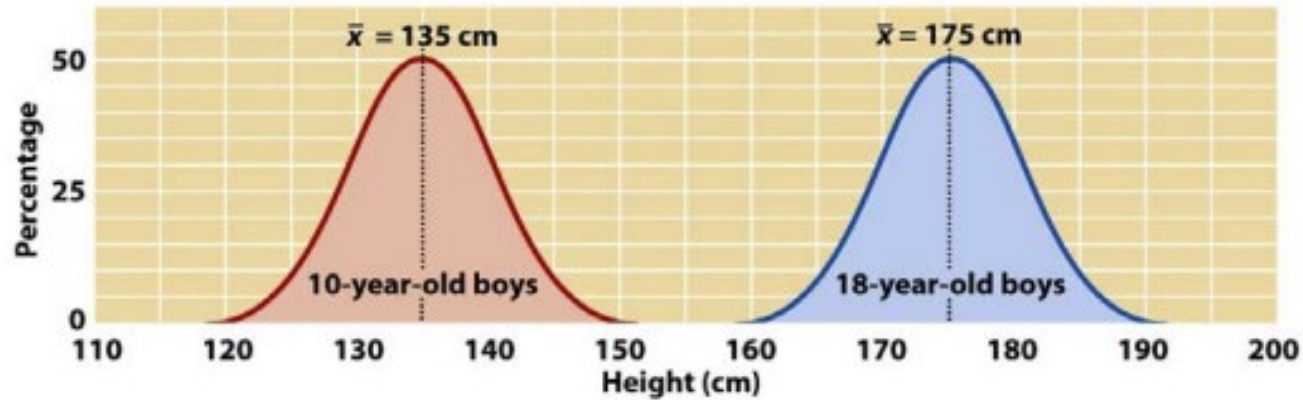


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Mean: sum of a collection of numbers divided by the count of numbers in the collection

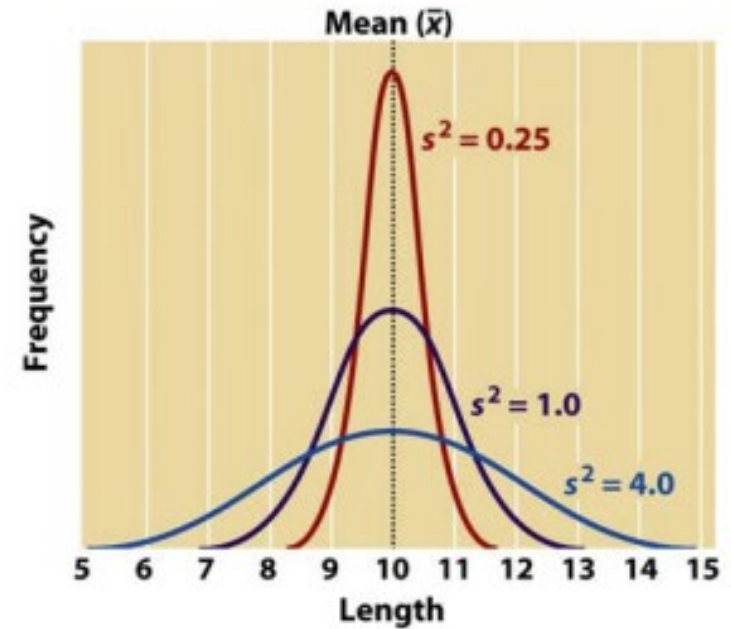


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Variance: measure of data dispersion (how far a set of numbers is spread out from their average value).

Number of gametes produced in the F₁ polyhybrid

Number of genotypes expected in F₂

Number of phenotypes expected in F₂

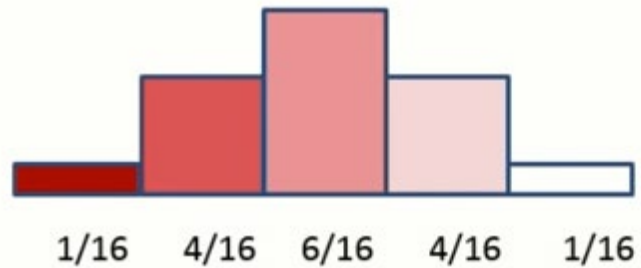
Number of individuals with parental phenotype expected in F₂

	1 locus	2 loci	3 loci	n loci
	2 (A,a)	4 (AB, ab, Ab, aB)	8 (ABC, ABc, Abc, abc, aBC, abC, AbC, aBc)	2ⁿ
	3 (AA, Aa, aa)	9 (AABB, AaBB, aaBB, AABb, AaBb, Aabb, aaBB, AAbb, aabb)	27 (AABBCC, ..., aaabbbccc)	3ⁿ
	3	5	7	2n+1
	1/4 (AA/aa)	1/16 (AABB/aabb)	1/64 (AABBCC/aabbcc)	1/4ⁿ

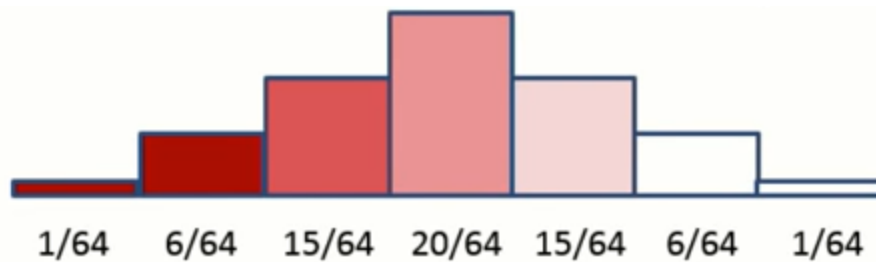
Calculating the number of genes involved in a quantitative trait



1 gene



2 genes



3 genes

AABBCCDDEE x aabbccdee

25 cm



15 cm

AaBbCcDdEe

20 cm

In a F_2 of 512, how many of them will have 19 cm?

AABBCCDDEE x aabbccdee

25 cm



15 cm

AaBbCcDdEe

20 cm

NUMBER OF ADDITIVE ALLELES	PHENOTYPE
0	15
1	16
2	17
3	18
4	19
5	20
6	21
7	22
8	23
9	24
10	25

AABBCCDDEE x aabbccdee

25 cm



15 cm

AaBbCcDdEe

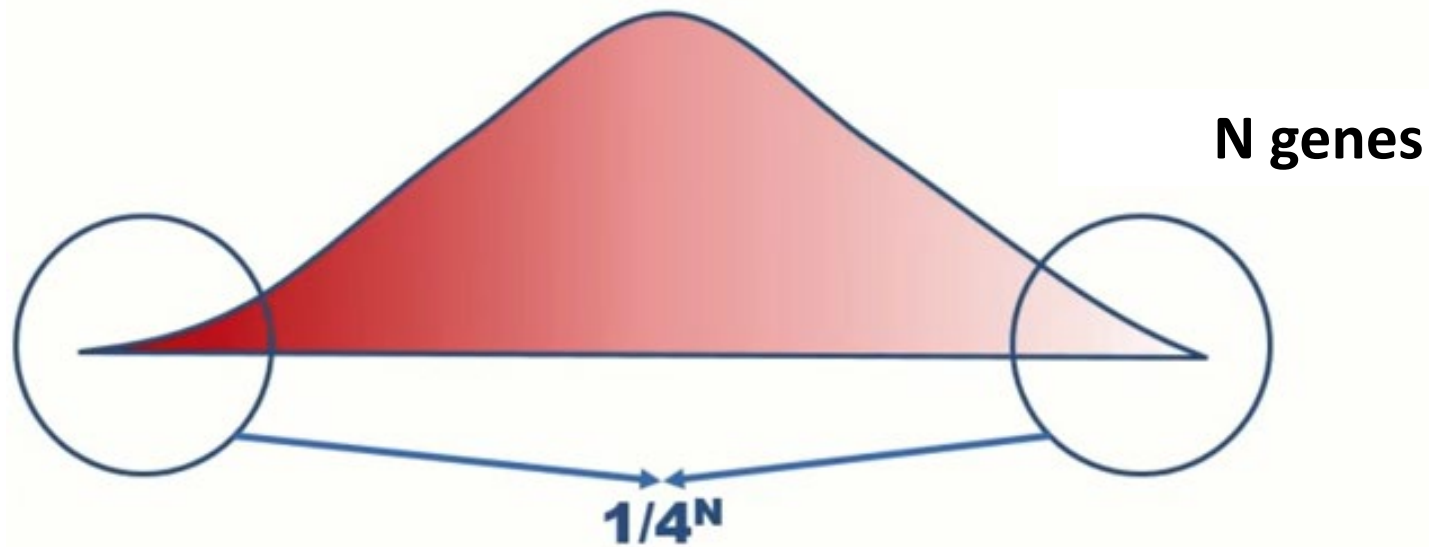
20 cm

$$\frac{10!}{4! 6!} (1/2)^4 \times (1/2)^8 = \frac{210}{1024} \times 512 = 105$$

Questions of Quantitative Genetics

- **How many genes** are involved in a particular trait?

Calculating the number of genes involved in a quantitative trait



$$p = 1/4^N$$

$$\rightarrow \text{Log}(p) = \log(1/4^N) \rightarrow \text{Log}(p) = N \log(1/4) \rightarrow$$

$$\rightarrow N = \text{Log}(p) / \log(1/4)$$

Calculating the number of genes involved in a quantitative trait

We have two purebreds plants producing fruits of 50g and 100g each.

F₁ is uniform and produces in average fruits of 75g.

F₂ is highly variable. 1 out of 1030 plants produces fruits of 50g.

$$\begin{aligned} \mathbf{N} &= \mathbf{Log(p) / log(1/4)} \rightarrow \mathbf{N = Log(1/1030) / log(1/4)} \rightarrow \\ &\rightarrow \mathbf{N = -3,013 / -0,602} \rightarrow \mathbf{N = 5,005} \end{aligned}$$

Questions of Quantitative Genetics

- What portion of observed variability is due to a **genetic differences** between individuals? What portion is due to **environmental factors**?

GENOTYPE (G) + ENVIRONMENT (E)  PHENOTYPE (P)

Heritability: estimates the degree of variation in a phenotypic trait in a population that is due to genetic variation between individuals in that population.

GENOTYPE (G) + ENVIRONMENT (E)  PHENOTYPE (P)

$$\mathbf{VAR(P) = VAR(G) + VAR(E) + VAR(G/E)}$$



Additive variance
Dominance variance
Gene-interaction variance

VAR(G/E): the expression of some genes relies on environmental factors.

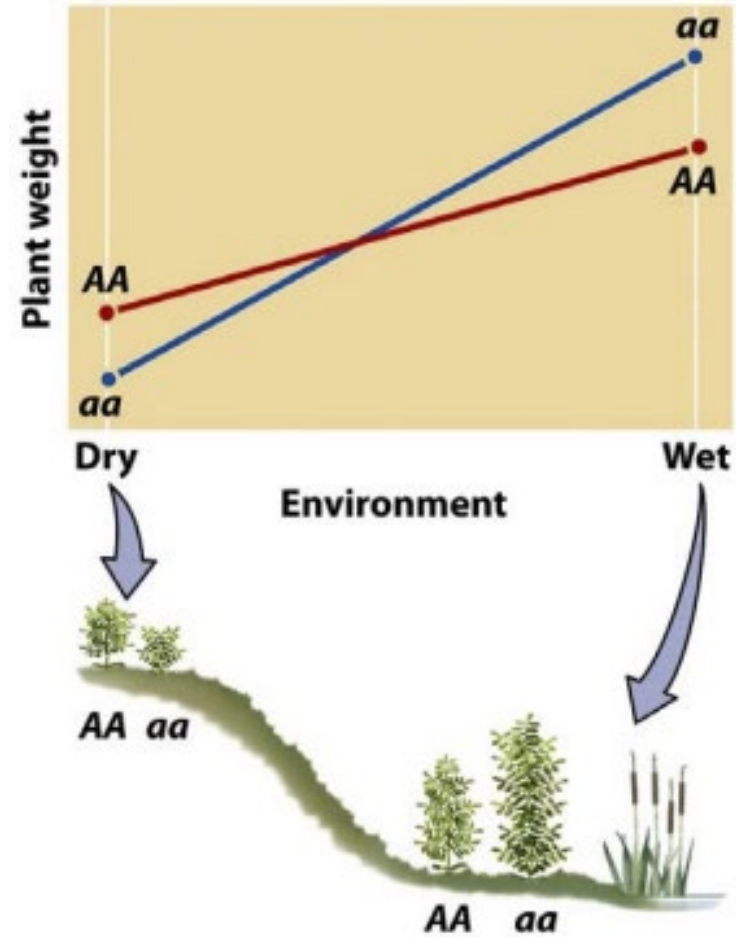


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Broad-sense heritability (H^2)

Reflects all the genetic contributions to a population's phenotypic variance including additive, dominant, and the one due to gene interactions.

$$H^2 = \frac{\text{Var}(G)}{\text{Var}(P)}$$

Calculating broad-sense heritability (H^2)

by elimination of some components of the equation.

$$\text{VAR}(P) = \text{VAR}(G) + \text{VAR}(E)$$

If all individuals are bred in an identical and controlled environment

$$\text{VAR}(E) = 0$$

$$\text{VAR}(P) = \text{VAR}(G)$$

$$H^2 = \frac{\text{Var}(G)}{\text{Var}(P)}$$

Calculating broad-sense heritability (H^2)

by elimination of some components of the equation.

$$\text{VAR}(P) = \text{VAR}(G) + \text{VAR}(E)$$

If all individuals are clones (genetically identical)

$$\text{VAR}(G) = 0$$

$$\text{VAR}(P) = \text{VAR}(E)$$

$$H^2 = \frac{\text{Var}(G)}{\text{Var}(P)}$$

Calculating broad-sense heritability (H^2)

by elimination of some components of the equation.

Experiment 1

We cultivate a type of plant and observe the size of the fruits. All variance will be considered VAR(P)

$$\text{VAR}(P) = \text{VAR}(G) + \text{VAR}(E) = 573$$

Experiment 2

We reproduce an individual asexually and observe the size of the fruits. All variance will be considered VAR(E)

$$\text{VAR}(P) = \text{VAR}(E) = 340$$

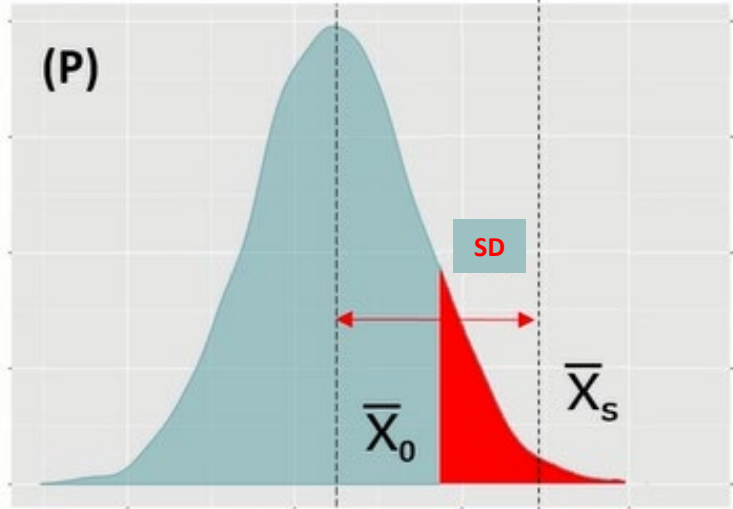
$$\text{VAR}(G) = \text{VAR}(P) - \text{VAR}(E) = 573 - 340 = 233$$

$$H^2 = \frac{\text{Var}(G)}{\text{Var}(P)} = \frac{233}{573} = 0.41$$

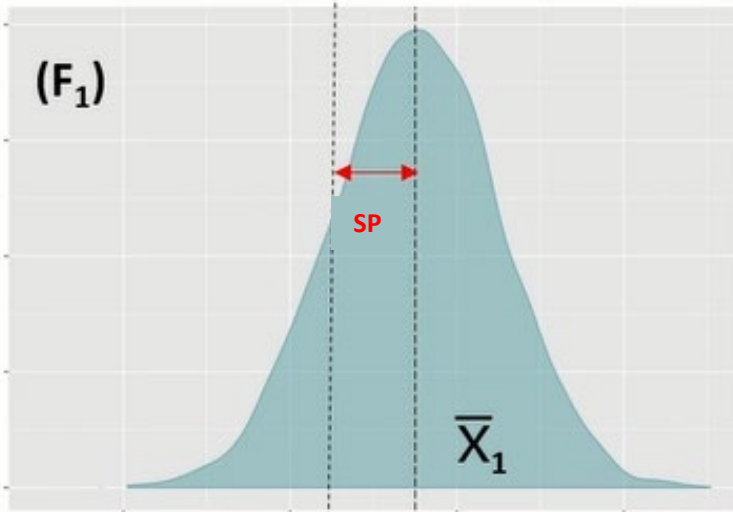
Narrow-sense heritability (h^2)

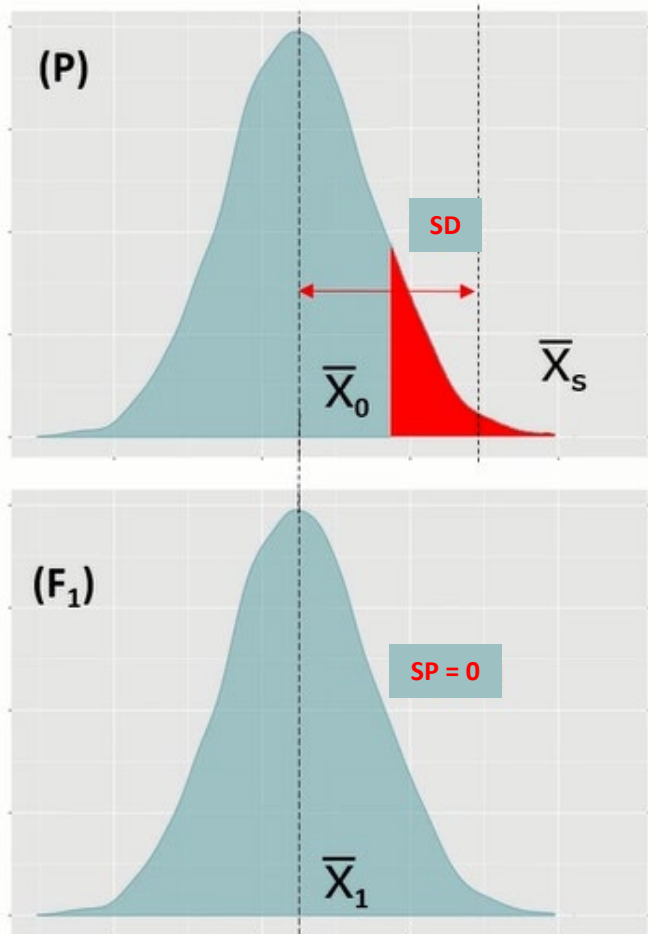
Reflects the genetic contribution of additive alleles to a population's phenotypic variance.

$$h^2 = \frac{\text{Var}(A)}{\text{Var}(P)}$$



$$h^2 = \frac{\text{selection progress}}{\text{selection differential}} = \frac{|x_1 - x_0|}{|x_s - x_0|}$$

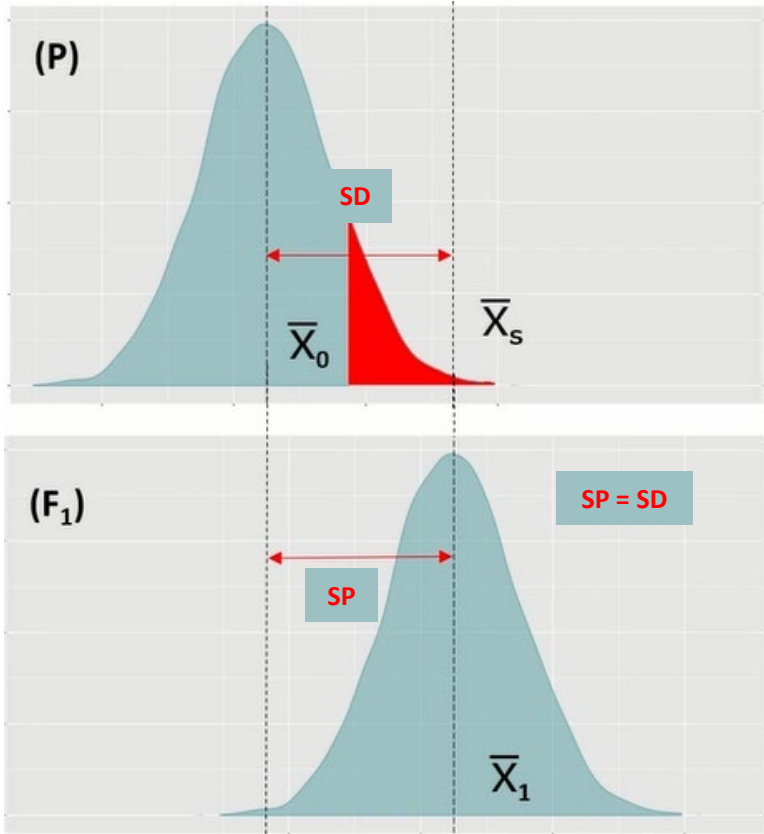




$$h^2 = \frac{\text{selection progress}}{\text{selection differential}} = \frac{|x_1 - x_0|}{|x_s - x_0|}$$

$$\frac{\overline{X}_1 - \overline{X}_0}{\overline{X}_s - \overline{X}_0} = 0$$

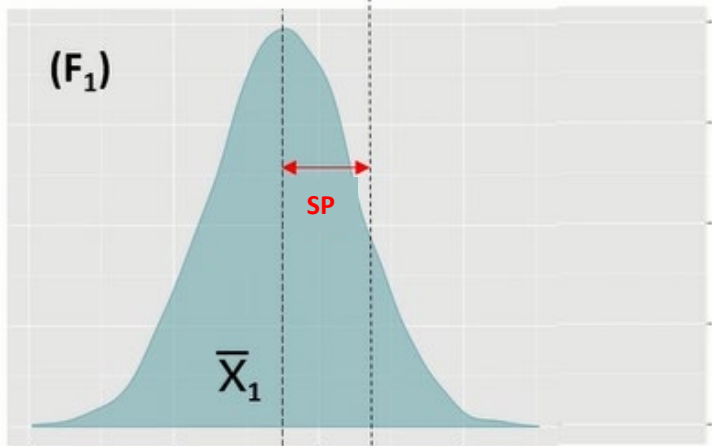
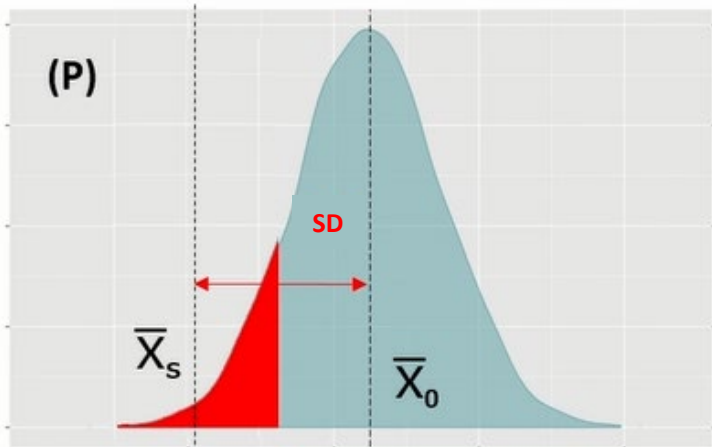
($\overline{X}_1 = \overline{X}_0$)



$$h^2 = \frac{\text{selection progress}}{\text{selection differential}} = \frac{|x_1 - x_0|}{|x_s - x_0|}$$

$$\frac{\overline{X}_1 - \overline{X}_0}{\overline{X}_s - \overline{X}_0} = 1$$

($\overline{X}_1 = \overline{X}_s$)



$$h^2 = \frac{\text{selection progress}}{\text{selection differential}} = \frac{|x_1 - x_0|}{|x_s - x_0|}$$

($\bar{X}_1 < \bar{X}_0$)

$$\frac{\bar{X}_1 - \bar{X}_0}{\bar{X}_s - \bar{X}_0}$$

($\bar{X}_s < \bar{X}_0$)

Heritability

$0 < h^2 < 0.25$	Low
$0.25 < h^2 < 0.5$	Medium
$0.5 < h^2 < 1$	High

In traits with **high heritability**, additive genetic component is predominant. They are easily improved.

In traits with **low heritability**, non-genetic components are more important in the expression of the character (environment). They are not easily improved.

Genetic Improvement

Can we improve a trait indefinitely?

- After many generations of selection, selection response stabilizes and the trait do not longer respond to selection.
- Genetic variability decreases in the population. Additive alleles get fixed. Heritability tends to 0.

Limitations of the heritability

- It is not individual but it refers to a specific population.
- There is no universal value of heritability for a particular trait.
- Even though heritability is high, influence of environment can still be important.

Questions of Quantitative Genetics

- Where are these genes **located in the genome?**

QTLs (Quantitative Trait Loci)

Chromosome regions involved in the expression of a polygenic trait.

If we find a molecular marker systematically inherited with a trait, this is most probably associated to a QTL.

Table 24.2 Quantitative characteristics for which QTLs have been detected

Organism	Quantitative Characteristic	Number of QTLs Detected
Tomato	Soluble solids	7
	Fruit mass	13
	Fruit pH	9
	Growth	5
	Leaflet shape	9
	Height	9
Corn	Height	11
	Leaf length	7
	Tiller number	1
	Glume hardness	5
	Grain yield	18
	Number of ears	9
	Thermotolerance	6
Common bean	Number of nodules	4
Mung bean	Seed weight	4
Cow pea	Seed weight	2
Wheat	Preharvest sprout	4
Pig	Growth	2
	Length of small intestine	1
	Average back fat	1
	Abdominal fat	1
Mouse	Epilepsy	2
Rat	Hypertension	2

